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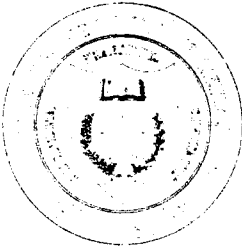
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**Bottom Backscatter from Trapped Bubbles**

Final Report under Contract N00039-91-C-0082,  
TD No. 01A1029, Bottom Backscatter from Trapped Bubbles

Frank A. Boyle  
Nicholas P. Chotiros

**Applied Research Laboratories**  
The University of Texas at Austin  
P. O. Box 8029 Austin, TX 78713-8029



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## **PREFACE**

This report is the final report of work that ARL:UT was tasked to perform under Contract N00039-91-C-0082, TD No. 01A1029, entitled Bottom Backscatter from Trapped Bubbles.



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## **1. INTRODUCTION**

The objective of this work is an improved model for high frequency acoustic backscatter from shallow water sediment at shallow grazing angles. Initial development of a model was accomplished by Boyle and Chotiros in 1992 (ARL-TR-92-12).<sup>1</sup> This work included studies of a Biot model for acoustic transmission and reflection, originally developed by Stern, Bedford, and Millwater.<sup>2</sup> Also included were the results of a comprehensive compilation of shallow grazing angle backscatter data. The compilation suggested, for some sediments, the possible importance of a new hypothetical mechanism for backscatter: resonant scattering from trapped bubbles. A preliminary model for acoustic backscatter from a spatial distribution of trapped bubbles in sediment was then presented.

This report contains improvements to the bubble backscatter model, including: (1) a method for modeling spherical acoustic sources in the water column, (2) incorporation of the Biot model in describing acoustic propagation through the sediment, and (3) an improved estimate of the trapped bubble size distribution function. This new model begins with a calculation of the pore pressure in the sediment, given a spherical acoustic source in the water column. This procedure is discussed in Section 2. Section 3 then describes how the backscattering strength of the sediment is computed. In Section 4, the resulting theoretical model is compared with experiment. A discussion of the results follows in Section 5.

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## 2. PORE PRESSURE

In this report we consider the pressure field generated by a point source in the water column above a sediment boundary, illustrated in Fig. 2.1. Of interest is the fluid pressure in the interstitial pores. This problem is treated by decomposing the spherical wavefield into a spectrum of plane waves. The technique follows the treatments of Brekhovskikh<sup>3</sup> and Westwood.<sup>4</sup> A Biot penetration model is used to calculate the transmission coefficient for each plane wave. The pore pressure is then obtained by summing the contributions of all plane waves.

### 2.1 PLANE WAVE DECOMPOSITION

The linear acoustic wave equation in a homogeneous medium with sound speed  $c$  is

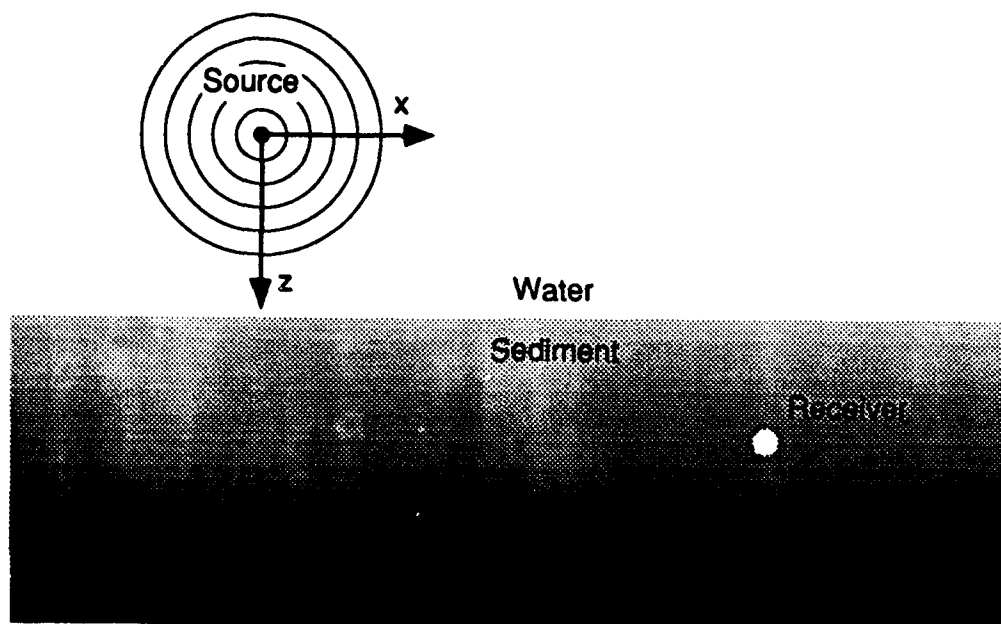
$$\nabla^2 p = \frac{1}{c^2} \frac{\partial^2 p}{\partial t^2} . \quad (2.1)$$

The solution to the above equation that describes the pressure field caused by a spherical source is

$$p = p_0 \frac{e^{i(kR - \omega t)}}{R} , \quad (2.2)$$

where  $R$  is the distance from the source,  $p_0$  the pressure amplitude at unit distance,  $t$  the time,  $\omega$  the angular frequency, and  $k=\omega/c$  the acoustic wave number. If the source is placed at the origin of a rectangular coordinate system, the distance  $R$  is given by  $R=(x^2+y^2+z^2)^{1/2}$ . If we set  $p_0$  to unity, suppress the time dependence  $e^{-i\omega t}$ , and confine ourselves to the  $z=0$  plane, the pressure field can be written as

$$p(x,y) = \frac{e^{ikr}}{r} , \quad (2.3)$$



**FIGURE 2.1**  
**SPHERICAL SOURCE ABOVE WATER-SEDIMENT BOUNDARY**

where  $r=(x^2+y^2)^{1/2}$ .

The pressure field can now be expanded in a double Fourier integral in the variables  $x$  and  $y$ ,

$$\frac{e^{ikr}}{r} = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} A(k_x, k_y) e^{i(k_x x + k_y y)} dk_x dk_y \quad (r \neq 0) \quad , \quad (2.4)$$

where  $A(k_x, k_y)$  is given by

$$(2\pi)^2 A(k_x, k_y) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \left( \frac{e^{ikr}}{r} \right) e^{-i(k_x x + k_y y)} dk_x dk_y \quad . \quad (2.5)$$

The above integral is more tractable in polar coordinates:

$$\begin{aligned} k_x &= q \cos \psi \\ k_y &= q \sin \psi \\ q &= (k_x^2 + k_y^2)^{1/2} \\ x &= r \cos \phi \\ y &= r \sin \phi \\ dx \, dy &= r \, dr \, d\phi \quad . \end{aligned}$$

In this coordinate system  $A(k_x, k_y)$  is given by

$$\begin{aligned} (2\pi)^2 A(k_x, k_y) &= \int_0^{2\pi} \int_0^{\infty} e^{ir[k - q \cos(\phi - \theta)]} dr \, d\phi \\ &= \int_0^{2\pi} \left[ \frac{e^{ir[k - q \cos(\phi - \theta)]}}{i[k - q \cos(\phi - \theta)]} \right]_{r=0}^{r=\infty} d\phi \quad . \end{aligned} \quad (2.6)$$

If there is some absorption, even if it is vanishingly small,  $k$  will have a positive imaginary part. In this case the quantity in brackets is zero when  $r = \infty$ . Therefore

$$\begin{aligned}
(2\pi)^2 A(k_x, k_y) &= \int_0^{2\pi} \frac{i d\phi}{[k - q \cos(\phi - \theta)]} \\
&= \frac{i}{k} \int_0^{2\pi} \frac{d\phi}{[1 - \frac{q}{k} \cos(\phi - \theta)]} \quad . \quad (2.6)
\end{aligned}$$

The integral in Eq. (2.6) is tabulated.<sup>5</sup> Upon substituting into Eq. (2.6), the following expression for  $A(k_x, k_y)$  is obtained:

$$A(k_x, k_y) = \frac{i}{2\pi\sqrt{k^2 - k_x^2 - k_y^2}} \quad . \quad (2.7)$$

Substitution of Eq. (2.7) into Eq. (2.4) yields

$$p(x, y) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \frac{i}{2\pi\sqrt{k^2 - k_x^2 - k_y^2}} e^{i(k_x x + k_y y)} dk_x dk_y \quad . \quad (2.8)$$

The above expression for the pressure field in the  $z=0$  plane can be generalized to describe the field in all space. This is done by multiplying the integrand by  $e^{ik_z z}$  for  $z>0$  or by  $e^{-ik_z z}$  for  $z<0$ .

$$p(x, y, z) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \frac{i}{2\pi\sqrt{k^2 - k_x^2 - k_y^2}} e^{i(k_x x + k_y y + k_z z)} dk_x dk_y, \quad (z \geq 0) \quad (2.9)$$

$$p(x, y, z) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \frac{i}{2\pi\sqrt{k^2 - k_x^2 - k_y^2}} e^{i(k_x x + k_y y - k_z z)} dk_x dk_y, \quad (z \leq 0) \quad (2.10)$$

where

$$k_z = \sqrt{k^2 - k_x^2 - k_y^2} \quad . \quad (2.11)$$

This "continuation" is justified because the integrand still satisfies the wave equation and because the new expressions reduce to the original expression Eq. (2.8) for the  $z=0$  plane when  $z$  approaches zero.

The integrals in Eq. (2.9) and Eq. (2.10) are over the entire  $k_x k_y$  plane. In order to span this plane, according to Eq. (2.11), imaginary values of  $k_z$  must be included. These so-called "inhomogeneous waves" attenuate exponentially with spatial dimension  $z$  and must be included to complete the construction of a spherical wavefield with plane waves.

In order to evaluate the integrals, Eq. (2.9) and Eq. (2.10), a transformation to spherical coordinates is made, as shown in Fig 2.2:

$$\begin{aligned} k_x &= k \sin\theta \cos\phi \quad , \\ k_y &= k \sin\theta \sin\phi \quad , \\ k_z &= k \cos\theta \quad . \end{aligned} \tag{2.12}$$

In the transformation the elemental area on the  $k_x k_y$  plane becomes

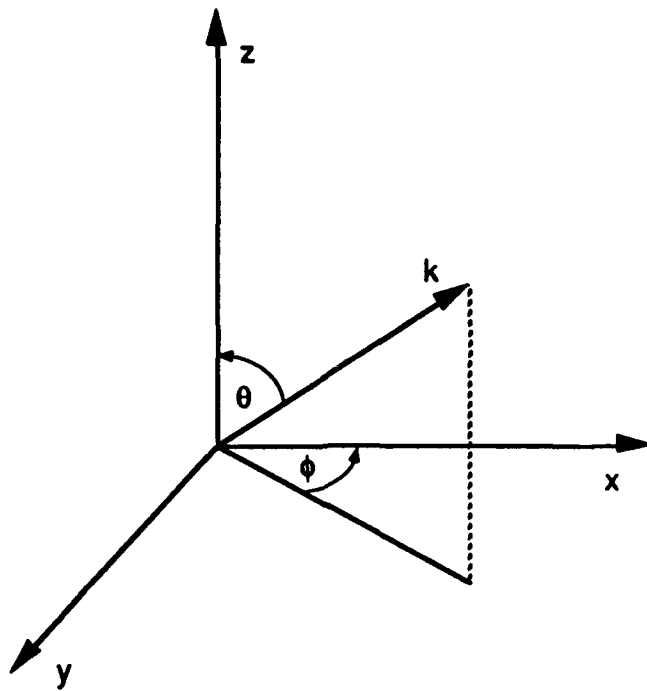
$$dk_x dk_y = (k \sin\theta d\phi)(k \cos\theta d\theta) \quad . \tag{2.13}$$

In order to cover the entire plane,  $\phi$  goes from 0 to  $2\pi$ . By allowing  $\theta$  to run from 0 to  $\pi/2$ , a disk on the plane of radius  $k$  is covered. In order to span the rest of the plane,  $\theta$  is further allowed to vary between  $\pi/2$  and  $\pi/2-i\infty$ . It would also have been possible to span the plane by letting  $\theta$  vary between  $\pi/2$  and  $\pi/2+i\infty$ , but this would have made the inhomogeneous waves *increase* in amplitude with increasing  $z$  instead of attenuating.

In the new coordinates, Eq. (2.9) becomes

$$p(x,y,z) = \frac{ik}{2\pi} \int_{\theta=0}^{\pi/2-i\infty} \int_{\phi=0}^{2\pi} e^{i(k_x x + k_y y + k_z z)} \sin\theta d\phi d\theta \quad , \quad (z \geq 0) \quad . \tag{2.14}$$





**FIGURE 2.2**  
**EXPRESSION OF WAVENUMBER  $k$  IN RECTANGULAR COORDINATES**

In order to determine the pressure field below the sediment interface, as in Fig. 2.3, each plane wave component must be multiplied by an appropriate plane wave transmission coefficient. The resulting pressure is given by

$$p(x,y,z) = \frac{ik}{2\pi} \int_{\theta=0}^{\frac{\pi}{2}-i\infty} \int_{\phi=0}^{2\pi} e^{i(k_x x + k_y y + k_z z_1 + k_{zs} z_2)} W(\theta) \sin\theta \, d\phi \, d\theta, \quad (z \geq 0), \quad (2.15)$$

where  $W$  is the transmission coefficient, which depends on the angle of incidence  $\theta$ .  $z_1$  is the height of the source,  $z_2$  is the depth of the receiver, and  $k_{zs}$  is the wavenumber in the lower medium. It can be shown that the integral over  $\phi$  is a Bessel function. This is done by first expressing the variables  $x$  and  $y$  in polar coordinates:

$$x = r \cos \phi_1, \quad y = r \sin \phi_1. \quad (2.16)$$

The integral over  $\phi$  can now be written as

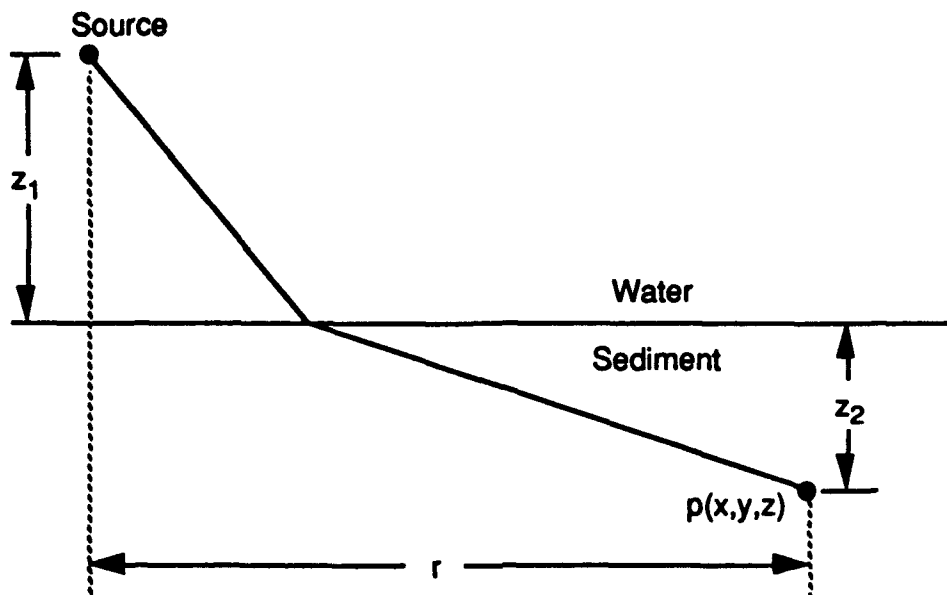
$$\begin{aligned} \int_{\phi=0}^{2\pi} e^{i(k_x x + k_y y)} d\phi &= \int_{\phi=0}^{2\pi} e^{ikr \sin\theta (\cos\phi_1 \cos\phi + \sin\phi_1 \sin\phi)} d\phi \\ &= \int_{\phi=0}^{2\pi} e^{ikr \sin\theta [\cos\phi_1 \cos(\phi - \phi_1)]} d\phi \\ &= 2\pi J_0(kr \sin\theta). \end{aligned} \quad (2.17)$$

By combining Eq. (2.14) and Eq. (2.16), a simplified expression for the pressure is obtained:

$$p(x,y,z) = \int_{\theta=0}^{\frac{\pi}{2}-i\infty} J_0(kr \sin\theta) e^{i(k_z z_1 + k_{zs} z_2)} W(\theta) \sin\theta \, d\theta. \quad (2.18)$$

## 2.2 INCORPORATION OF BIOT MODEL

In order to solve Eq. (2.18) for the pressure below the sediment boundary, the transmission coefficient  $W(\theta)$  and vertical wavenumber  $k_{zs}$  in the sediment must be specified. For this purpose the Biot penetration model



**FIGURE 2.3**  
**PRESSURE FIELD BELOW WATER-SEDIMENT INTERFACE**

described in ARL-TR-92-12<sup>6</sup> was used. This model was originally developed by Stern, Bedford, and Millwater<sup>7</sup> and later modified to treat gassy sediments. This was done by varying the complex compressibility and density of the pore fluid. The gas contribution to these parameters was obtained using a theory developed by Hawkins<sup>8</sup> involving reflection coefficients from bubble distributions.

The Biot model differs from traditional ways of treating acoustic media in that it allows for two phases: a solid skeletal phase through which a fluid phase is allowed to flow freely. It is based on the following coupled pair of equations of motion:

$$\mu \nabla^2 \mathbf{u} + (H - 2\mu) \nabla(\nabla \cdot \mathbf{u}) - C \nabla(\nabla \cdot \mathbf{w}) = \rho \ddot{\mathbf{u}} - \rho_f \ddot{\mathbf{w}} \quad (2.19)$$

$$C \nabla(\nabla \cdot \mathbf{u}) - M \nabla(\nabla \cdot \mathbf{w}) = \rho_f \ddot{\mathbf{u}} - (c_p/\beta) \ddot{\mathbf{w}} - (F\eta/\kappa) \dot{\mathbf{w}}, \quad (2.20)$$

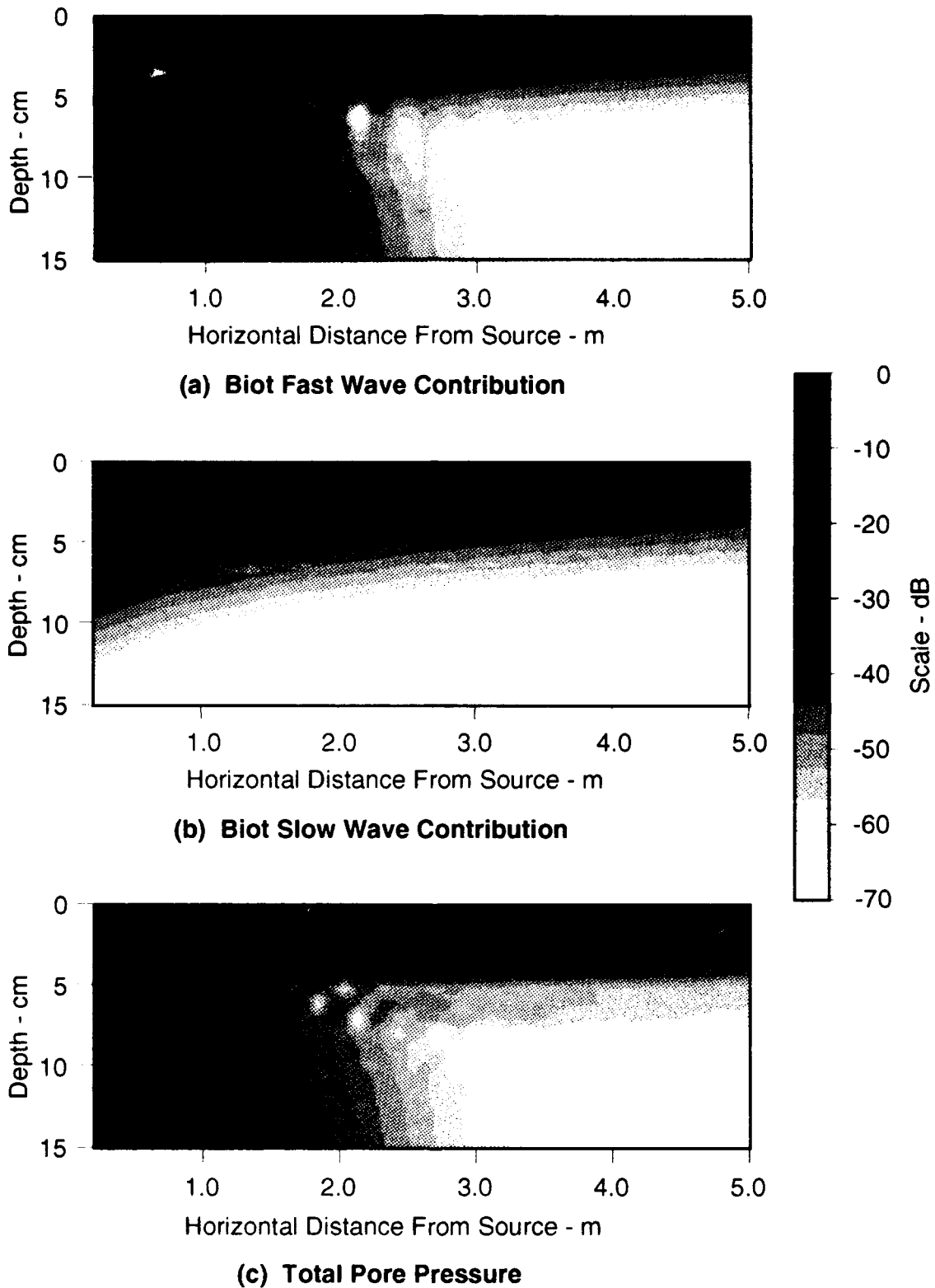
where  $\mathbf{u}$  and  $\mathbf{w}$  are the fluid and solid displacements,  $\mu$  is the fluid viscosity,  $\rho_f$  and  $\rho$  are the mass densities of fluid and saturated sediment, respectively,  $k$  is the permeability, and  $F$  is a constant that accounts for the frequency dependence of the drag force between fluid and solid. The constants  $H$ ,  $C$ , and  $M$  are determined by the compressibilities of the fluid and solid constituents.

One important feature of the Biot model is that it predicts two compressional waves in the medium, in addition to a shear wave. For the faster of these waves, the fluid moves generally in phase with the solid part of the medium. For the slow wave the two components move out of phase. Usually the slow waves can be neglected and single phase models can be used to model ocean sediments. Under certain conditions, however, slow waves appear to be dominant. Such is the case when a wavefront is incident upon a sediment half space at a grazing angle less than the critical angle for the fast wave.

The above described Biot penetration model calculates, for any complex angle of incidence  $\theta$ , the pore pressure transmission coefficient  $W(\theta)$  and vertical wavenumber  $k_{zs}$ . The transmission coefficient  $W(\theta)$  is obtained from

simultaneous solution of equations (51-54) of Stern *et al.* The fast and slow vertical wavenumbers  $k_{zs}$  are given by Eq. (59) and Eq. (60), respectively.

Equation (2.18) is then calculated numerically, given  $W(\theta)$  and  $k_{zs}$ . Figure 2.4 is a plot of the computed pore pressure in the sediment, given the input parameters of Table 2.1. The pressure contributions are broken down according to the types of waves involved. Wavespeeds of 1690 m/s for the fast wave and 1170 m/s for the slow wave are predicted, with attenuations of 12.2 and 41.2 dB/m, respectively. It is clear that the slow wave has a pressure amplitude that is not negligible in comparison to that of the fast wave, particularly when the horizontal distance to the acoustic source is large. Hence the effects of the slow wave must be included in predicting total pressures in the sediment as well as backscattered pressures from the sediment.



**FIGURE 2.4**  
**PORE PRESSURES DUE TO 30 kHz SPHERICAL SOURCE**  
**AT HEIGHT OF 50 cm ABOVE BOTTOM**

**TABLE 2.1**  
**PENETRATION MODEL INPUT PARAMETERS**

Fluid Density	1000	kg/m <sup>3</sup>
Fluid Bulk Modulus	$2.0 \times 10^9$	Pa
Porosity	0.4	
Grain Density	2650	kg/m <sup>3</sup>
Pore Size	$1.0 \times 10^{-5}$	m
Viscosity	$1.0 \times 10^{-3}$	kg/m-s
Permeability	$1.0 \times 10^{-10}$	m <sup>2</sup>
Grain Bulk Modulus	$9.0 \times 10^9$	Pa
Frame Shear Modulus	$2.61 \times 10^7$	Pa
Shear Logarithmic Decrement	0.15	
Frame Bulk Modulus	$4.36 \times 10^9$	Pa
Bulk Logarithmic Decrement	0.15	
Virtual Mass Parameter	1.25	
Gas Bulk Modulus	$2.48 \times 10^5$	Pa
Bubble/Pore Radius Ratio	0.06	
Gas Content	0	

### 3. SEDIMENT BACKSCATTERING STRENGTH

#### 3.1 CALCULATION OF BACKSCATTERING STRENGTH BY RECIPROCITY

Consider the situation illustrated in Fig. 3.1. In Appendix A an approximation for the backscattered pressure amplitude  $p_2$  at A from a scatterer at B is derived:

$$p_2 = \sqrt{\frac{\sigma}{4\pi} \frac{p_1^2}{p_0}} \quad (3.1)$$

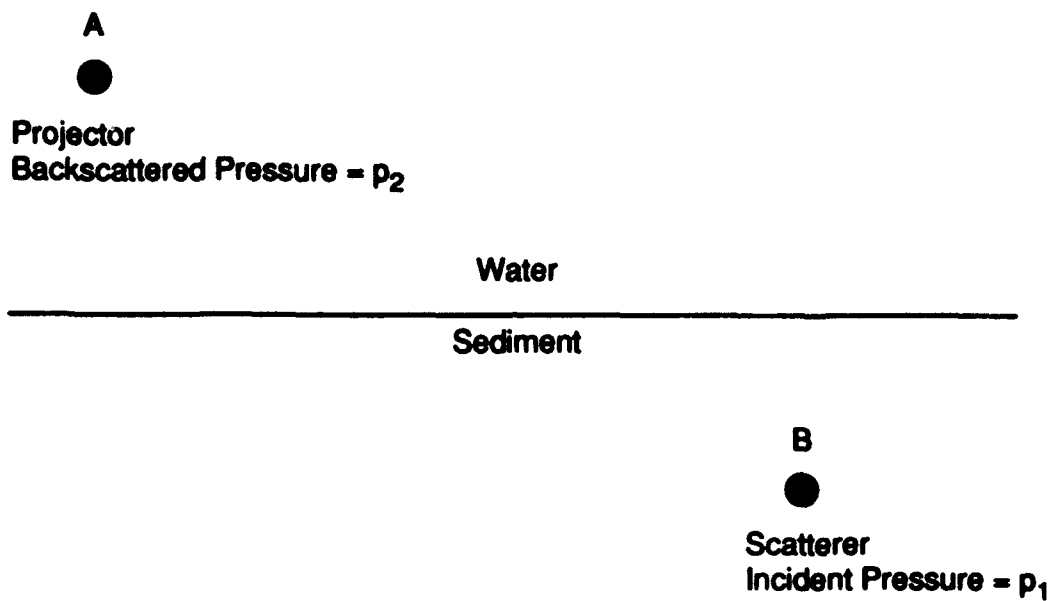
where  $\sigma$  is the effective cross section of the scatterer, defined as the area which, when multiplied by the incident intensity, equals the total scattered power. The incident pressure amplitude generated by the source at a distance of 1 m in the water column is  $p_0$ , and  $p_1$  is the pressure generated at the scatterer, located at B.

In this analysis, the sediment is a medium with many scatterers throughout its volume. A mean scattering cross section per unit volume  $\sigma_{bv}$  can be computed, given the scattering cross sections and population densities of the contained scatterers. If a projector at A insonifies a volume element  $dx dy dz$  at B, the returned pressure at A is

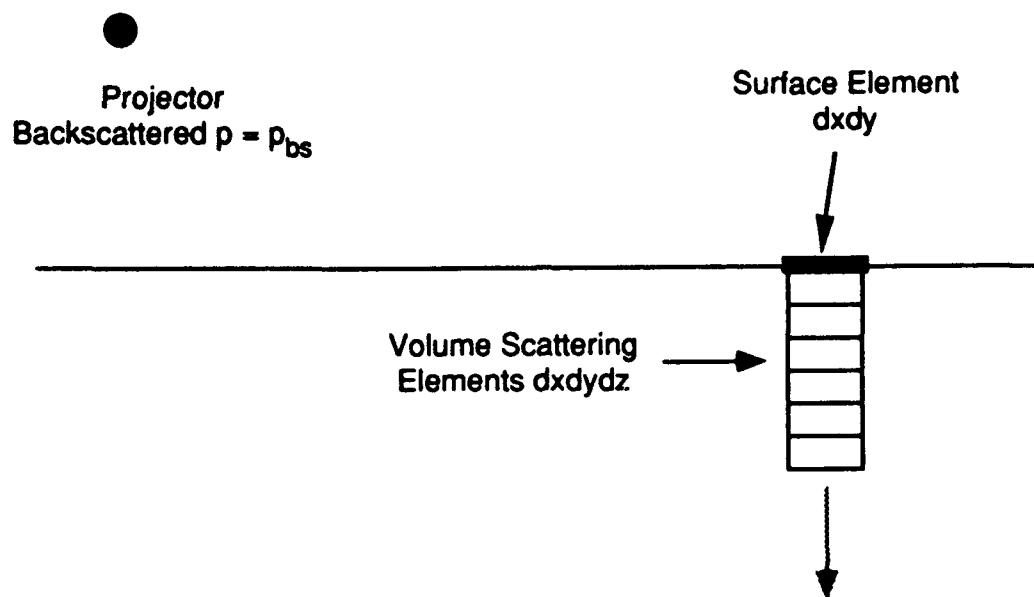
$$p_2 = \sqrt{\frac{\sigma_{bv} dx dy dz}{4\pi} \frac{p_1^2}{p_0}} \quad (3.2)$$

The scattering can be treated as a function of location along the water-sediment interface, as in Fig. 3.2. In this case, the backscattered intensity from a surface element  $dx dy$  is the sum of all backscatter contributions from the sediment volume below the surface element  $dx dy$ . The total mean square backscattered pressure per unit surface area is given by





**FIGURE 3.1**  
**BACKSCATTER AT A FROM SINGLE SCATTERER AT B**



**FIGURE 3.2**  
**BACKSCATTER FROM THE VOLUME**  
**BELOW SURFACE ELEMENT  $dx dy$**

$$p_{bs}^2 = \int_0^{\infty} \frac{\sigma_{bv}}{4\pi} \frac{p_1^4}{p_0^2} dz \quad (3.3)$$

Figure 3.3 illustrates the computation of the backscattering strength of a surface element. The backscattering strength is

$$BS = 10 \log \left( \frac{p_s^2}{p_o'^2} \right) \quad (3.4)$$

where  $p_s$  is the root mean square scattered pressure at unit radius from the surface element and  $p_o'$  is the incident pressure at the surface element. The incident pressure  $p_o'$  is

$$p_o' = p_o / R \quad (3.5)$$

where  $R$  is the distance from the source to the surface element. The scattered pressure at unit radius is obtained from the scattered pressure  $p_{bs}$  at the source,

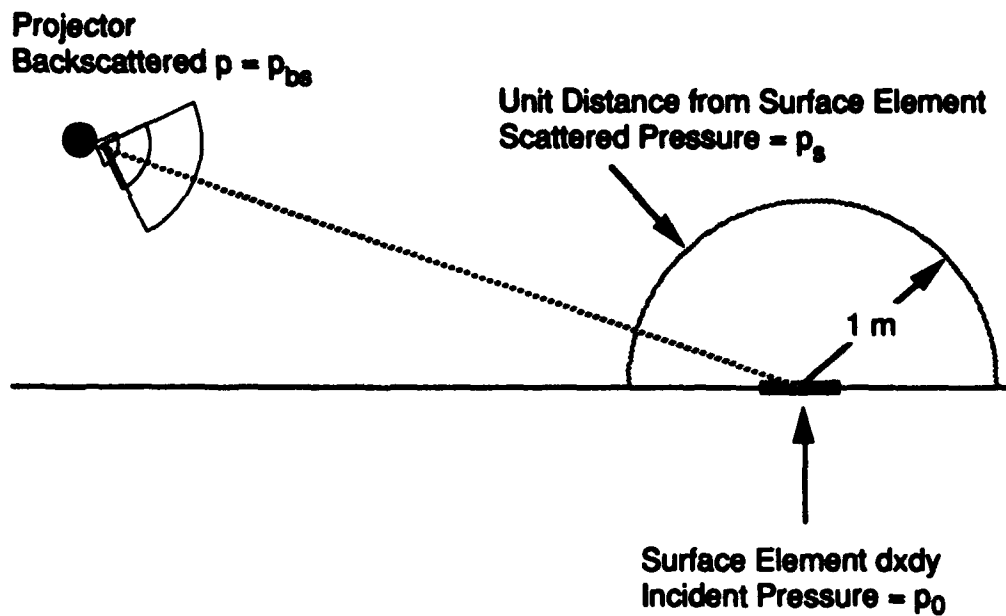
$$p_s = p_{bs} R \quad (3.6)$$

By combining Eqs. (3.3) - (3.6), the backscattering strength is expressible as a function of  $\sigma_{bv}$ ,  $R$ ,  $p_o$ , and  $p_1$ .

$$BS = 10 \log \frac{R^4}{4\pi p_o^4} \int_0^{\infty} \sigma_{bv} p_1^4 dz \quad (3.7)$$

### 3.2 DETERMINATION OF SEDIMENT VOLUME SCATTERING CROSS SECTION $\sigma_{bv}$

In order to find the backscattering strength via Eq. (3.7), it is necessary to calculate  $\sigma_{bv}$ , the backscattering cross section per unit volume of sediment.



**FIGURE 3.3**  
**CALCULATING THE BACKSCATTERING STRENGTH**  
**FROM SURFACE ELEMENT  $dxdy$**

Since the hypothetical mechanism for scattering in this model is bubble resonant backscatter,  $\sigma_{bv}$  can be expressed as follows:

$$\sigma_{bv} = \int_0^{\infty} f_b(r_b) \sigma(r_b) dr_b \quad , \quad (3.8)$$

where  $f_b(r_b)$  is the spatial distribution function of bubbles, defined as the number of bubbles per unit volume per unit radius increment about the radius  $r_b$ , and  $\sigma(r_b)$  is the scattering cross section of a single bubble of radius  $r_b$ . Expressions for  $\sigma(r_b)$  and  $f_b(r_b)$  are developed in subsections 3.2.1 and 3.2.2.

In developing the model, three assumptions are made:

- (1) A bubble's size is regulated by the pore in which it is found; i.e., the ratio of bubble radius to pore radius is constant. This assumption is necessary to permit an estimate of the bubble size distribution in the absence of other information.
- (2) The possibility of multiple scattering between bubbles is neglected. Justification for this assumption is included in Appendix B.
- (3) The bubbles act as though they were spherical, isolated, and surrounded by water. The effects of the interaction between bubbles and between bubbles and the walls of the pores are neglected.

There is some experimental and theoretical support for this approximation. Howkins<sup>9</sup> predicted and measured the resonance frequencies of bubbles near rigid boundaries. Two configurations were studied, one involving a bubble near a semi-infinite rigid plane and another involving a bubble contained inside a rigid cylindrical cup. In neither case was there a dramatic influence on the bubble's resonance frequency. Resonance frequencies decreased by 15% for the plane boundary and 50% for the cylindrical cup. A bubble

trapped between sand grains might act similarly, being more confined than a free bubble near a semi-infinite plane but less confined than one inside a cylindrical cup.

### 3.2.1 Estimate of Single Bubble Backscattering Cross Section

Equation (3.8) requires that  $\sigma(r_b)$ , the single bubble backscattering cross section, be specified. The scattering cross section for a single spherical bubble of radius  $r_b$  insonified by a signal of frequency  $f$  is given by Wildt:<sup>10</sup>

$$\sigma_r(r_b) = \frac{4\pi r_b^2}{\left[\left(\frac{f_r}{f}\right)^2 - 1\right]^2 + \delta^2} \quad (3.9)$$

$\delta$  is a damping constant and  $f_r$  is the resonance frequency, given by Minneart<sup>11</sup>

$$f_r = \frac{1}{2\pi r_b} \left( \frac{3\gamma P}{\rho} \right)^{1/2} \quad (3.10)$$

where  $\gamma$ ,  $P$ , and  $\rho$  are the ratio of specific heats, pressure, and density, respectively, of the medium inside the bubble. Medwin<sup>12</sup> showed that, for resonant bubbles,  $r_b f_r$  is approximately 3 and  $\delta$  is approximately 0.1. It is convenient to work in terms of the variable  $v = \ln(r_b)$  instead of  $r_b$ . In this notation the single bubble scattering cross section is

$$\sigma_v(v) = \frac{4\pi e^{2v}}{\left[\left(\frac{f_r}{f}\right)^2 - 1\right]^2 + \delta^2} \quad (3.11)$$

### 3.2.2 Estimate of Bubble Size Distribution

Equation (3.8) requires that the bubble size distribution function  $f_b(r_b)$  be specified. Our approach is to first obtain a pore volume distribution function. A

bubble distribution function is then found by assuming that bubbles always occupy a constant fraction of the available pore space, in accordance with assumption (1) stated previously.

### Pore Size Distribution Function

Finney and Wallace<sup>13</sup> investigated the formation of pores between randomly packed identical spheres. Figure 3.4 is a histogram of the distribution of interstitial pore radii for an aggregate of spheres. It can be approximated as a bimodal distribution function  $p(x,y)$  where  $x$  and  $y$  are the natural logarithms of the grain and pore radii, respectively. For any value of  $x$ ,  $p(x,y)$  is approximated by a sum of two normal distributions.

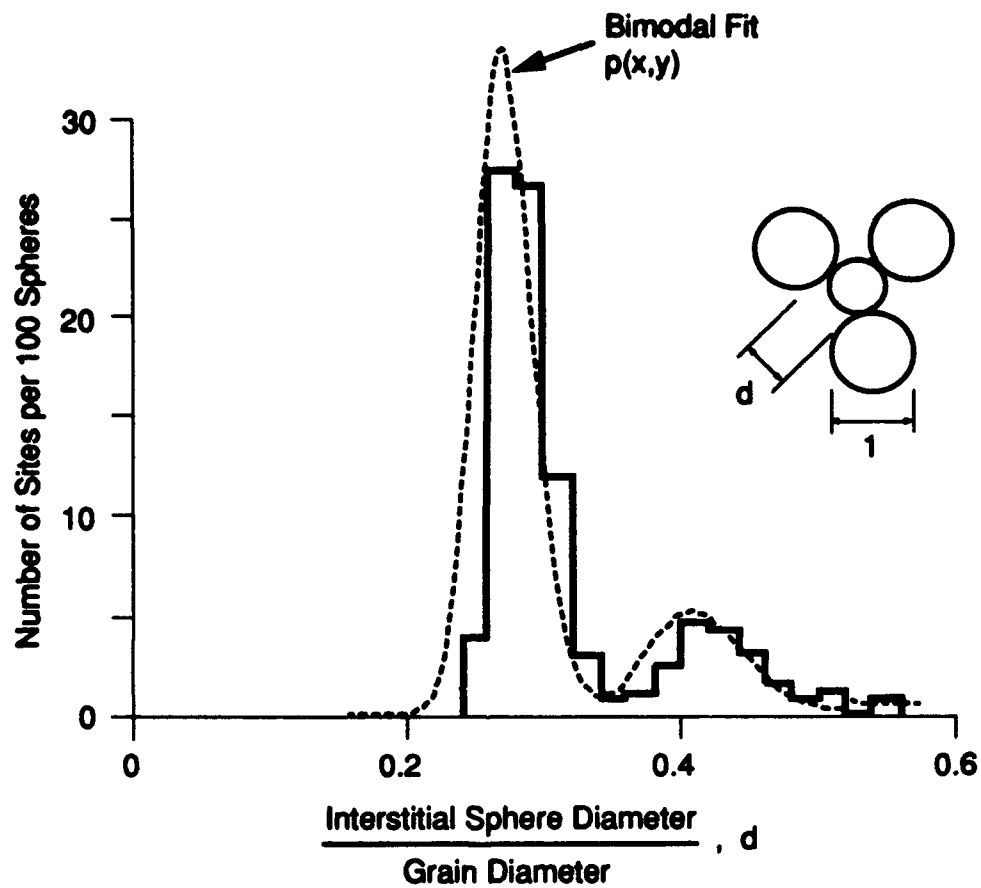
$$p(x,y) = A \left[ \frac{1}{\sqrt{2\pi} b_1} e^{-\frac{(y-x-a_1)^2}{2b_1^2}} \right] + B \left[ \frac{1}{\sqrt{2\pi} b_2} e^{-\frac{(y-x-a_2)^2}{2b_2^2}} \right] \quad , \quad (3.12)$$

where  $a_i$  is the mean and  $b_i$  is the standard deviation of the  $i$ th peak.

Sediments have a measurable particle size distribution function  $f_x(x)$ , where  $x = \log(\text{grain radius})$ . A pore size distribution function  $f_p(y)$  is estimated by convolving this function with  $p(x,y)$ :

$$f_p(y) = f_x(x) * p(x,y) \quad . \quad (3.13)$$

In writing Eq. (3.13) we are neglecting the possibility that particles of varying sizes pack differently than those of a single size. For example, small particles may occupy the pores created between larger particles. An assumption is also made that irregular sediment grains pack like perfect spheres. The justification behind proceeding with these assumptions comes from the measured porosities of sandy sediments. Porosities between 0.36 and 0.4 are common for sandy sediments. This compares closely with a porosity of 0.363 for randomly packed identical spheres.<sup>14</sup>



**FIGURE 3.4**  
**DISTRIBUTION OF INTERSTITIAL SPHERE SIZES**  
**FOR DENSE RANDOM PACKING OF HARD SPHERES**  
**OF UNIT DIAMETER**



## Bubble Size Distribution Function

Assumption (1) states that a bubble's radius is governed by the size of the surrounding pore. This means that the bubble size distribution  $f_b(v)$ , where  $v$  is the natural log of the bubble radius, will reflect the pore size distribution  $f_p(v)$ :

$$f_b(z) = \xi f_p(v - \ln(R_{bp})) \quad . \quad (3.14)$$

$R_{bp}$  is a constant equal to the ratio of a bubble's radius to that of its surrounding pore. It is assumed that each pore may hold only one gas bubble, and that the fraction of pores that indeed have gas bubbles is  $\xi$ . In the absence of any further information, it will be assumed that  $\xi$  is a constant independent of pore size. The gas fraction  $\zeta$  is obtainable by dividing the total volume of bubbles by the porosity:

$$\zeta = \frac{\int_{-\infty}^{\infty} \frac{4}{3} \pi e^{3v} f_b(v) dv}{\beta} \quad . \quad (3.15)$$

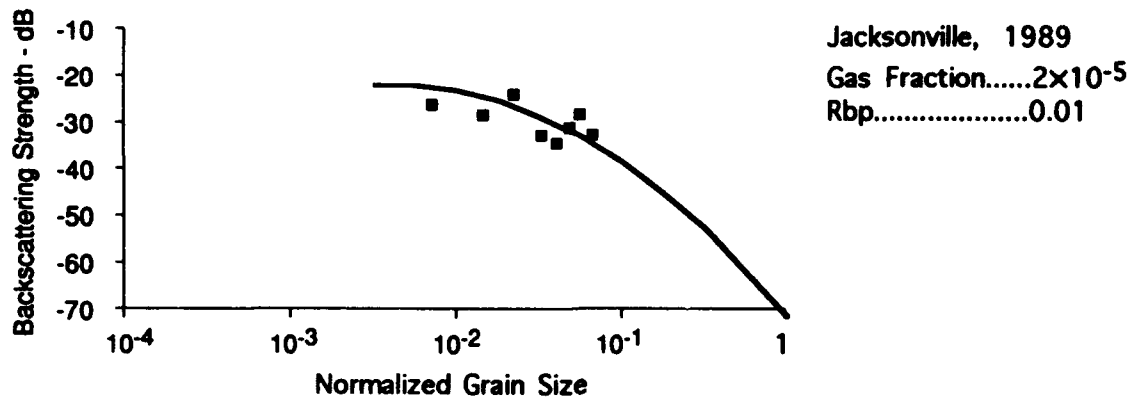
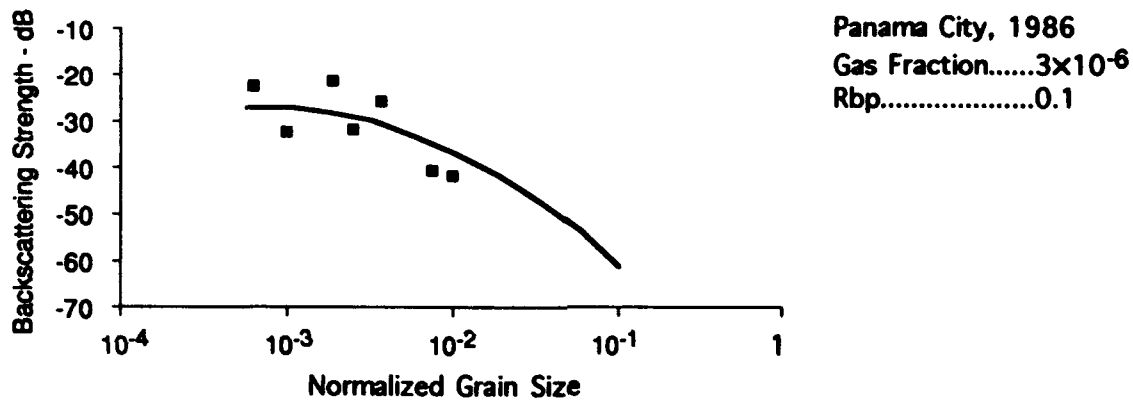
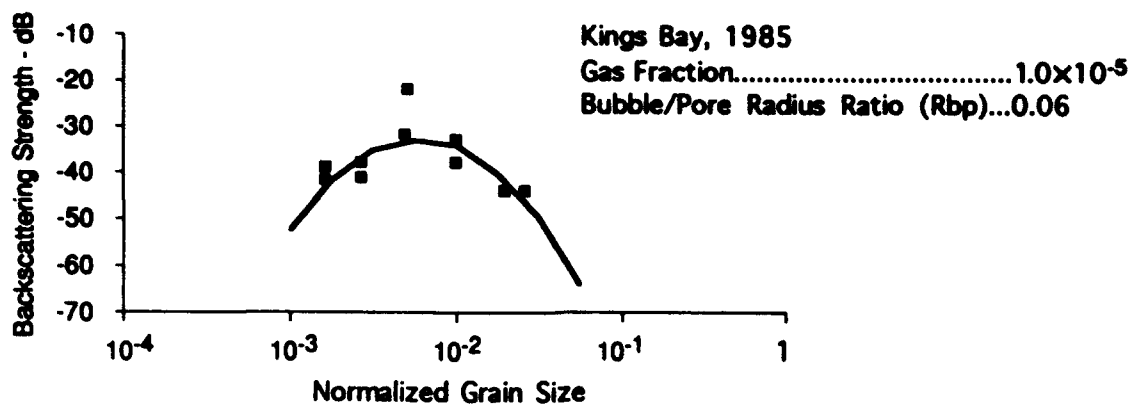
In this analysis  $R_{bp}$  and  $\zeta$  are treated as free parameters and are varied to fit the model to experimental data.

#### **4. COMPARISON OF THEORY WITH EXPERIMENT**

In Fig. 4.1 comparisons are made between the predictions of the backscatter model and experimental measurements of the backscattering strength taken over three selected sites. The input parameters for each site are listed in Table 4.1. In each case a best fit was obtained by varying the gas fraction  $\zeta$  and the bubble-to-pore radius ratio  $R_{bp}$ . The resulting gas fractions are annotated and varied between  $1 \times 10^{-5}$  and  $3 \times 10^{-6}$ .

The model predicts a peak in the backscattering strength at a frequency that corresponds to resonance for the bubbles in the distribution. The width of this peak will depend on the width of the bubble size distribution. The backscattering strength will decrease with increasing frequencies that are greater than resonance. In this respect the model differs from other current models, which always predict an increase in backscattering strength with increasing frequency.

At present the model is still being developed and these results must be regarded as preliminary. An improved estimate of the compressibility of the gassy fluid phase is being developed. An estimate of the acoustic impedance of the fluid constrained in the sediment pores is also being incorporated. These changes to the model will probably change the amplitudes of the predicted backscattering strengths in Fig. 4.1. The overall features, i.e., the broad maximum in backscattering strength at bubble resonance and the model's sensitivity to very small gas fractions, are not expected to change.



**FIGURE 4.1**  
**COMPARISON OF EXPERIMENTAL DATA**  
**WITH BACKSCATTERING STRENGTHS**  
**PREDICTED BY EQ. (3.7)**

**TABLE 4.1**  
**BACKSCATTER MODEL INPUT PARAMETERS**

<b>Site</b>		<b>Kings Bay 1985</b>	<b>Panama City 1985</b>	<b>Jacksonville 1989</b>
Fluid Density	(kg/m <sup>3</sup> )	1000	1000	1020
Fluid Bulk Modulus	(Pa)	2.25×10 <sup>9</sup>	2.25×10 <sup>9</sup>	2.406×10 <sup>9</sup>
Porosity		0.3633	0.3906	0.3793
Grain Density	(kg/m <sup>3</sup> )	2656	2650	2650
Grain Radius	(m)	3.896×10 <sup>-4</sup>	1.593×10 <sup>-4</sup>	5.586×10 <sup>-4</sup>
Viscosity	(kg/m-s)	1.0×10 <sup>-3</sup>	1.0×10 <sup>-3</sup>	1.0×10 <sup>-3</sup>
Permeability	(m <sup>2</sup> )	1.0×10 <sup>-10</sup>	1.0×10 <sup>-10</sup>	1.0×10 <sup>-10</sup>
Grain Bulk Modulus	(Pa)	9.0×10 <sup>9</sup>	9.0×10 <sup>9</sup>	1.06×10 <sup>10</sup>
Frame Shear Modulus	(Pa)	2.61×10 <sup>7</sup>	2.61×10 <sup>7</sup>	2.57×10 <sup>7</sup>
Shear Log Decrement		0.15	0.15	0.15
Frame Bulk Modulus	(Pa)	4.36×10 <sup>9</sup>	4.36×10 <sup>9</sup>	4.36×10 <sup>9</sup>
Bulk Log Decrement		0.15	0.15	0.15
Virtual Mass Parameter		1.25	1.25	1.25
Gas Bulk Modulus	(Pa)	2.48×10 <sup>5</sup>	2.48×10 <sup>5</sup>	2.48×10 <sup>5</sup>
Bubble/Pore Radius Ratio		0.06	0.1	0.01
Gas Content		1.0×10 <sup>-5</sup>	3×10 <sup>-6</sup>	2×10 <sup>-5</sup>

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## **5. CONCLUSION**

A heuristic model for high frequency acoustic backscatter from sandy sediments based on bubble resonance behavior has been developed. This model is consistent with the broad backscattering strength maximum observed in some of the experimental data and demonstrates that a trapped bubble backscattering mechanism may be significant in high frequency acoustic backscatter from sediments.

The analysis demonstrates that gas bubbles are a likely cause of observed backscatter from sediments. Very small gas fractions of between  $1 \times 10^{-5}$  and  $3 \times 10^{-6}$  are necessary. Since there is no direct way to measure gas fractions this small, an independent verification of this analysis is required, which is difficult.

The assumption that the bubble size is proportional to the pore size was made to allow a first estimate of the bubble size distribution. Further research is required to determine a more precise relationship between pore geometry and bubble size.

The effects of Biot slow and fast compressional waves have been included. The results show that at very shallow grazing angles the slow wave's amplitude is significant in comparison to that of the fast wave. This suggests that a complete description of shallow grazing angle penetration must include the effects of the slow wave. For this reason the Biot theory appears to be most appropriate in acoustic modeling in this regime.

At present, work is in progress in improving the backscatter model. An expression for the backscattering cross section for trapped bubbles is being developed. This will allow elimination of the assumption that trapped bubbles scatter as though they existed in an unbounded medium. Further improvements will include studies of grain packing structures and their relationships to trapped bubble sizes and geometries.

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**APPENDIX A**  
**RECIPROCITY PRINCIPLE**



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Consider the situation illustrated in Fig. A.1. According to the reciprocity principle, the sound pressure at B when a source is placed at A is the same as that produced at A when the same source is placed at B. In the case where sound from a source at A encounters a scatterer at B, the scatterer can be regarded as another source whose sound pressure can be measured back at A. In this case, a signal propagating along the return path experiences the same loss that the original incident signal did on its way to B. Let a cw source at A cause a complex pressure  $p_1$  to exist at B. The scatterer at B will return a complex pressure  $p_2$  at A, given by:

$$p_2 = (p_1 \zeta) \left( \frac{p_1}{p_0} \right) , \quad (\text{A.1})$$

where  $p_1 \zeta$  is the pressure generated by the scatterer, measured at a unit distance from the scatterer. The incident pressure generated by the source at a distance of 1 m in the water column is  $p_0$ .  $\zeta = re^{i\theta}$  is a complex factor related to the scattering cross section. Let the time dependent complex pressures  $p_0$ ,  $p_1$ ,  $p_2$  be expressed as

$$\begin{aligned} p_0 &= p_0 e^{i(\theta_0 \omega t)} \\ p_1 &= p_1 e^{i(\theta_1 \omega t)} \\ p_2 &= p_2 e^{i(\theta_2 \omega t)} , \end{aligned} \quad (\text{A.2})$$

where  $p_1$ ,  $p_2$ , and  $p_3$  are moduli and  $\theta_1, \theta_2$ , and  $\alpha \nu \delta \theta_3$  are phases of the complex pressures  $p_0$ ,  $p_1$ , and  $p_2$ . Upon substitution into Eq. (A.1),

$$p_2 e^{i(\theta_2 \omega t)} = \left( p_1 e^{i(\theta_1 \omega t)} r e^{i\theta} \right) \left( \frac{p_1 e^{i(\theta_1 \omega t)}}{p_0 e^{i(\theta_0 \omega t)}} \right) . \quad (\text{A.3})$$

Upon taking a time average of Eq. (A.3),

A  
●  
Projector  
Backscattered Pressure  
Amplitude =  $p_2$

B  
●  
Scatterer  
Incident  
Pressure  
Amplitude =  $p_1$

**FIGURE A.1**  
**BACKSCATTER AT A FROM SINGLE SCATTERER AT B**

$$p_2 \langle e^{i(\theta_2 - \omega t)} \rangle = r \frac{p_1^2}{p_0} \langle e^{i(\theta + 2\theta_1 - \theta_0 - \omega t)} \rangle \quad (A.4)$$

The factor  $r$  is related to the scattering cross section  $\sigma$  as follows:

$$r = \sqrt{\frac{\sigma}{4\pi}} \quad (A.5)$$

where  $\sigma$  is defined as the area which, when multiplied by the incident intensity, equals the total scattered power. Upon substituting Eq. (A.5) into Eq. (A.4) and noting that the time averages of the bracketed quantities in Eq. (A.4) are unity,

$$p_2 = \sqrt{\frac{\sigma}{4\pi}} \frac{p_1^2}{p_0} \quad (A.6)$$

The situation in Fig. 3.1 differs from that in Fig. A.1 in that the scatterer exists under a fluid-sediment boundary. The above derivation leading up to Eq. (A.6) rests on the assumption that both scatterer and projector exist in the same medium. For the case in which the scatterer is below a sediment boundary, an impedance mismatch between fluid and sediment must be accounted for. In this analysis, such a mismatch is neglected. As a result, Eq. (A.6) can only be considered an approximation. The approximation should be reasonable since the trapped bubbles that act as scatterers exist in the trapped fluid within the sediment pores. Effectively, the assumption is being made that the interstitial fluid has the same acoustic impedance as the fluid above the sediment.

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**APPENDIX B**  
**JUSTIFICATION OF SINGLE SCATTERING MODEL**

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Attenuation in sediment is caused by absorption and scattering of an incident acoustic wave. The single scattering approximation is valid when the absorption contribution is large in comparison with the scattering contribution. In practical terms this criterion is considered satisfied when the single scattering albedo<sup>15,16</sup> is less than 0.2. The albedo  $a$  is defined as

$$a = \frac{\sigma_s}{\sigma_e} \quad , \quad (B.1)$$

where  $\sigma_s$  is the scattering cross section per unit volume and  $\sigma_e$  is the extinction cross section per unit volume. Each bubble in the sediment will act as a scatterer with scattering cross section  $\sigma_s$  given by Eq. (3.9):

$$\sigma_s(r_b) = \frac{4\pi r_b^2}{\left[ \left( \frac{f_r}{f} \right)^2 - 1 \right]^2 + \delta^2} \quad . \quad (B.2)$$

The total bubble scattering cross section per unit volume  $\sigma_s$  is this expression integrated over the distribution of bubble radii:

$$\sigma_s = \int_0^\infty \sigma_s(r_b) f(r_b) dr_b \quad . \quad (B.3)$$

The extinction cross section  $\sigma_e$  associated with the same bubble is<sup>17</sup>

$$\sigma_e(r_b) = \frac{4\pi r_b^2 \left( \frac{\delta}{k_r r_b} \right)}{\left[ \left( \frac{f_r}{f} \right)^2 - 1 \right]^2 + \delta^2} \quad . \quad (B.4)$$

where  $K_r$  is the acoustic wavenumber at resonance,

$$k_r = \frac{2\pi f_r}{C} \quad . \quad (B.5)$$



The total extinction cross section per unit volume is the integral of Eq. (B.4) over the bubble size distribution.

$$\sigma_e = \int_0^\infty \sigma_e(r_b) f(r_b) dr_b \quad , \quad (B.6)$$

Upon inserting expressions (B.3) and (B.6) into expression (B.1) above, the single scattering albedo is given by

$$a = \frac{\int_0^\infty \sigma_s(r_b) f(r_b) dr_b}{\int_0^\infty \sigma_e(r_b) f(r_b) dr_b} \quad . \quad (B.7)$$

The integral in the numerator can be expressed as a sum of resonant and nonresonant contributions. The nonresonant part is negligible except in the case of very large bubbles. The remaining resonant contribution includes a delta function about the resonance radius. The value of this integral can therefore be approximated by simply evaluating the integrand at the resonance radius.

Computation of the albedo via expression (B.7) is nontrivial. In determining whether a single scatter model applies, however, it suffices simply to determine if the albedo is less than 0.2. The numerator can be estimated accurately by neglecting the nonresonant contribution as described above. If the denominator is approximated similarly, i.e., by evaluating its integrand at the resonance radius, any error incurred will make the denominator smaller. An approximate albedo, which can be defined as

$$\tilde{a} = \frac{\sigma_s(a_r)}{\sigma_e(a_r)} \quad , \quad (B.8)$$

will therefore be greater than or equal to the actual albedo given in expression (B.7). Therefore, if the approximate albedo  $\tilde{a}$  is less than 0.2, a single scattering

model is sufficient. Upon combining Eq. (B.2), Eq. (B.4), and Eq. (B.8),  $\tilde{a}$  becomes

$$\tilde{a} = \frac{k_r r_b}{\delta} \quad . \quad (B.9)$$

Medwin<sup>18</sup> showed that, for resonant bubbles,  $f_r a_r$  is approximately 3 and  $\delta$  is approximately 0.1. If these values are used,  $\tilde{a}$  is evaluated at 0.126. A single scattering model is therefore appropriate.

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